## COURSES OF STUDY FOR MATHEMATICS SUBSIDIARY (Approved by Academic Council)

## **DEPARTMENT OF MATHEMATICS**



# MARWARI COLLEGE, RANCHI

(AN AUTONOMOUS & CONSTITUENT UNIT OF RANCHI UNIVERSITY) COLLEGE WITH POTENTIAL FOR EXCELLENCE SELECTED BY UGC Website : marwari-college.org

## Full Marks: 400

## Number of Semesters: 4

## Number of Papers: 4

## B. Sc. Subsidiary. Part - I: 200 Marks (2 Papers)

## B. Sc. Subsidiary. Part - II: 200 Marks (2 Papers)

DISTRIBUTIONS OF MARKS IN MATHEMATICS SUBSIDIARY						
Academic year	Semester		Theory paper	Full marks	Pass marks	Duration
First year	Ι		(A) Differential Calculus	100	33	3 Hrs.
		1	(B) Set Theory			
			(C) Analytic Geometry of Two Dimensions			
			(D) Real Analysis			
	II	2	(A) Integral Calculus	100	33	3 Hrs.
			(B) Vectors			
			(C) Analytic Geometry of Three Dimensions			
			(D) Advance Real Analysis			
Second year	III	3	(A) Abstract Algebra	100	33	3 Hrs.
			(B) Differential Equations			
			(C) Probability & Statistics			
			(D) Trigonometry			
	IV	4	(A) Advance Abstract Algebra			
			(B) Complex Variable	100	33	3 Hrs.
			(C) Matrix			
			(D) Mechanics			

[Q:01]

## B.Sc. Part – I (Mathematics Subs.) Semester – I PAPER – 1

#### Time: 3 Hrs.

Pass Marks: 33

#### Full Marks: 100 Instructions :

Answer ten questions selecting atleast one from each group. Each question contains two parts : Part (a) & Part (b). Part (a) is of short answer type questions (e.g. definition, statement, simple problems). It will be of 3 marks. Part (b) is of long answer type questions (e.g. Theorems, Problems etc.). It will be of 7 marks. [Atleast 50% questions should be theoretical]

## Group - A: <u>DIFFERENTIAL CALCULUS</u> [L : 12, Q : 04]

- Successive differentiation, nth derivatives of some standard functions. Leibnitz' theorem. [Q:01]
- Expansion of functions, Taylor's infinite series, Maclaurin's series, Application of Taylor's and Maclaurin's series, Partial Differentiation.

[Q:01]

• Tangents and Normal and their equations in Cartesian from , Parametric Form, Tangents at origin, angle of intersection between two curves, length of tangent, sub tangent, Normal, Subnormal.

[Q:02]

## Group – B: <u>SET THEORY</u> [L : 12, Q : 04]

- Indexed family of sets, Generalised set of operations & De-Morgan's laws, set mapping. [O:01]
- Relations of the set, equivalence relations & fundamental theorem on equivalence relation. [Q:01]
- Partial order relation, concept of 1. u. b. & g. l. b., infimum & supremum of a set, maximal & minimal elements. [Q:01]
- Countable and uncountable sets.

## Group - C: <u>ANALYTICAL GEOMETRY OF TWO DIMENSIONS</u> [L : 12, Q : 04]

- Change of rectangular axes ,Changing of the origin without changing the direction of the axes , Change of direction of the axes without changing the origin. [Q:02]
- Reduction of the equation of second degree to represent a parabola, ellipse and hyperbola, Equation of the tangent and normal. [Q:02]

### Group - D: <u>REAL ANALYSIS</u> [L : 12, Q : 04]

• Fundamental and Algebraic properties of the set of real numbers, Neighbourhoods and limit points of a set, Completeness property, Archimedean Property, density theorem for the set of real numbers, Bounded sets, Open Sets, Closed sets and compact sets, Bolzano-Weirstras' theorem. Connectedness and Compactness, Heine-Borel theorem.

[Q:02]

• Limit and continuity : Limit, Continuity, Uniform Continuity, Properties of continuous functions in closed intervals, Functions of bounded Variation.

[Q:02]

### **REFERENCES:**

- 1. Diff. Calculus Das & mukherjee / Lalji Pd.
- 2. Set theory K. K. Jha / Lalji Pd
- 3. Analytical geometry of two dimension Jagdish Jha / Lalji pd.
- 4. Real Analysis K. K. Jha / Lalji Pd.

5. Mathematical Analysis - Shanti Narayan.

## B.Sc. Part – I (Mathematics Subs.) Semester – II PAPER – 2

Full Marks: 100

## Time: 3 Hrs.

Pass Marks: 33

#### Instructions :

Answer ten questions selecting atleast one from each group. Each question contains two parts : Part (a) & Part (b). Part (a) is of short answer type questions (e.g. definition, statement, simple problems). It will be of 3 marks. Part (b) is of long answer type questions (e.g. Theorems, Problems etc.). It will be of 7 marks. [Atleast 50% questions should be theoretical]

### Group - A : <u>INTEGRAL CALCULUS</u> [L : 12, Q : 04]

- Integration of rational and irrational functions.
- [Q:01]
- Evaluation of definite integral, Properties of Definite Integral.
- [Q:01]
- Curve tracing, Length and area.
  - [Q:01]
- Volume and Surface area of solids of revolution. [Q:01]

## Group – B: <u>VECTOR ANALYSIS</u> [L : 12, Q : 04]

- Product of three and four vectors.
- [Q:01]
- Application to Geometry & mechanics Work done, moment of a vector about a fixed point and about a line.
  - [Q:01]
- Vector Differentiation : Differentiation of a vector function of a scalar variable, Gradient, Divergence, Curl and Second order operators in Cartesian coordinate system. [Q:02]

### Group – C: <u>ANALYTIC GEOMETRY OF THREE DIMENSIONS</u> [L : 12, Q : 04]

- Rectangular, Spherical-Polar and Cylindrical coordinates. [Q:01]
- Direction cosines, angle between straight lines, [Q:01]
- Equation of planes. [Q:01]
- Equation of straight lines, shortest distance between straight lines. [Q:01]

## Group – D: <u>ADVANCE REAL ANALYSIS</u> [L : 12, Q : 04]

- **SEQUENCE :** Monotonic sequences, bounded sequence, Convergence sequence, limit of sequences, Limit supremum, limit infimum, Cauchy sequence, General Principle of Convergence. [Q:02]
- Convergence and divergence of series of real numbers, Pringsheim's theorem, Comparison tests, Cauchy's root test, D Alembert's ratio test, Rabbe's test, De-Morgan's and Bertrand Test, Logarithmic test.

[Q:01]

• Alternating series, Leibnitz Test, Absolute convergent series. [Q:01]

#### **REFERENCES:**

- 1.
- 2.
- Integral calculus Das & Mukherjee/ Lalji Pd. Vector Analysis Lalji Prasad/ Shanti Narayan Mathematical Analysis Shanti Narayan/ S.C. Mallick Real Analysis K. K. Jha / Lalji Pd. 3.
- 4.
- 5. Analytical Geometry of Three Dimension - J.T. Bell/ J. Jha

## B.Sc. Part – II (Mathematics Subs.) Semester – III PAPER – 3

## Full Marks: 100

## Time: 3 Hrs.

Pass Marks: 33

#### Instructions :

Answer ten questions selecting atleast one from each group. Each question contains two parts : Part (a) & Part (b). Part (a) is of short answer type questions (e.g. definition, statement, simple problems). It will be of 3 marks. Part (b) is of long answer type questions (e.g. Theorems, Problems etc.). It will be of 7 marks. [Atleast 50% questions should be theoretical]

## Group - A: <u>ABSTRACT ALGEBRA</u> [L : 12, Q : 04]

- Binary operations, Notion of group, Abelian group and non abelian group with examples. Different ways of defining a group, Concept of subgroup and cyclic group, coset, Lagrange's theorem.
- Homomorphism and Isomorphism, Fundamental theorem of homomorphism, Cayley's theorem

[Q:02]

### Group - B : <u>DIFFERENTIAL EQUATIONS</u> [L:12, Q : 04]

• First order higher degree, Clairaut's from . Singular Solution, Orthogonal trajectories

[Q:02]

- Linear Equations with constant coefficients, Homogeneous linear equations with variable coefficients. [Q:01]
- Simultaneous equation dx/ P= dy/Q= dz/R and total d.e. Pdx+Qdy+Rdz= 0, together with their geometrical significance. [Q:01]

## Group – C: <u>PROBABILITY & STATISTICS</u> [L : 12, Q : 04]

• Notion of Probability : Random experiment, sample space, axiom of probability, elementary properties of probability, equally likely outcome problems, dependent and independent events, conditional and unconditional probability, Baye's theorem.

#### [Q:02]

- Co-efficient of Correlation, Rank, correlation & spearman's formula, [Q:01]
- Curve fitting and method of least squares, Lines of regression, Regression coefficients and their properties. [Q:01]

#### Group – D: TRIGONOMETRY [L : 12, Q : 04]

• De Moivre's Theorem and its application in expansions. Exponential, and trigonometric functions of complex numbers, Properties of exponential and Trigonometric function of a complex number, Euler's theorem, Periodicity Trigonometric function. Logarithm of complex quantities. Hyperbolic functions: Relations between hyperbolic and circular function, Relation between inverse Hyperbolic and inverse circular functions.

[Q:02]

• Gregory's Series, Evaluation of  $\pi$ .

#### **REFERENCES:**

- 1. Abstract Algebra Surjeet Singh and Quasi Zmeeruddin
- 2. Modern Algebra A. R. Vasishtha & A. K. Vasishtha
- 3. Differential Equation Lalji Prasad/ M.D. Raisinghania
- 4. Probability & Statistics S.C. Gupta & V.K. Kapoor/ J.N. Kapoor
- 5. Elementary Statistical Methods Goongupta & Dasgupta
- 6. Trigonometry Das & Mukherjee/ Lalji Prasad

[Q:02]

## B.Sc. Part – II (Mathematics Subs.) Semester – IV PAPER – 4

## Full Marks: 100

### Time: 3 Hrs.

Pass Marks: 33

#### Instructions :

Answer ten questions selecting atleast one from each group. Each question contains two parts : Part (a) & Part (b). Part (a) is of short answer type questions (e.g. definition, statement, simple problems). It will be of 3 marks. Part (b) is of long answer type questions (e.g. Theorems, Problems etc.). It will be of 7 marks. [Atleast 50% questions should be theoretical]

## Group –A: <u>ADVANCE ABSTACT ALGEBRA</u> [L : 12, Q : 04]

• Concepts of ring, Sub ring, Ideal, Integral domains and Field, Ring Homomorphism and isomorphism. [Q:04]

## Group –B : <u>COMPLEX\_VARIABLE</u> [L : 12, Q : 04]

• Functions of a Complex variables Limit, Continuity, derivative, Cauchy- Riemann Equations, Analytic function, Harmonic function, Construction of Analytic Function, Milne-Thompson Mehtod.

[Q:04]

## Group - C : <u>MATRIX</u> [L : 12, Q : 04]

• **Matrices** : Definition, Triangular Matrices, Singular, non singular, symmetric, skew symmetric, Transpose, Conjugate, adjoint of a matrix, inverse of a matrix, Hermitian and skew Hermitian Matrices, Orthogonal, unitary matrices.

[Q:02]

• Law of operations, partitioning.

[Q:01]

• Elementary transformation, Normal form, elementary matrices, rank of product, equivalence of matrices and criteria for equivalence. Determination of rank of a Matrix, General solution of AX=B.

[Q:01]

### Group –D: <u>MECHANICS</u> [L : 12, Q : 04]

- Conditions for equilibrium of coplanar forces, Astatic Centre. [Q:02]
- Kinematics in two dimensions : Tangential, normal, radial, transverse velocities and acceleration, Angular Velocity and Acceleration, S.H.M.

[Q:02]

#### **REFERENCES:**

- 1. Modern Algebra A. R. Vasishtha & A. K. Vasishtha/ Surjeet Singh & Quasi Zammeeruddin
- 2. Complex Aalysis E. T. Copsion / Lalji Prasad/ J.N. Sharma.
- 3. Matrix Shanti Narayan

- Statics Das & Mukherjee.
  Dynamics-Das & Mukherjee.